



## Measuring and Modelling Seiche Phenomena in NSW Harbours

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### Outline of Presentation

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- Brief history of Seiche measurement and modelling in NSW
- Forcing functions
- Numerical modelling of seiche phenomena in NSW-New Developments Such as Wavelet Analysis
- Physical modelling of Seiche phenomena in NSW-Past Errors and New Developments
- Role of seiche analysis in future development of harbours
- Summary



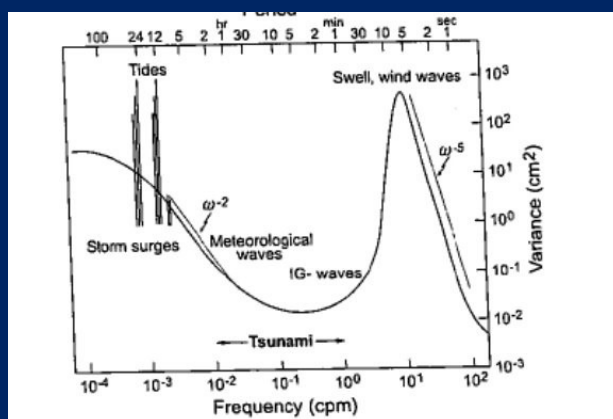
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## Extreme Coastal Seiche in Various Regions of the World (Rabinovich-1996)

- Japan-Nagasaki Bay->4m,35min
- China-Longkou Harbour>2.5m,2h
- Spain-Ciudadella Harbor>4.0m,10.5min
- Canada-Newfoundland-2.0m-3.0m,10-40 min
- Netherlands-Rotterdam Harbour>1.5m,85-100min

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## Relative energy of swell, tide and seiche waves



'The most conspicuous thing about long waves in the open ocean is their absence.' Prof. Munk, Scripps

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## NSW Offshore Waverider buoy network and location of harbours



| Wave Station  | Date Site Commissioned | Directional Buoy Deployed |
|---------------|------------------------|---------------------------|
| Byron Bay     | 14-Oct-1976            | 26-Oct-1999               |
| Coffs Harbour | 26-May-1976            | 14-Feb-2012               |
| Crowdy Head   | 10-Oct-1985            | 19-Aug-2011               |
| Sydney        | 17-Jul-1987            | 03-Mar-1992               |
| Port Kembla   | 07-Feb-1974            | 20-Jun-2012               |
| Batemans Bay  | 27-May-1986            | 23-Feb-2001               |
| Eden          | 08-Feb-1978            | 16-Dec-2011               |

- 7 Datawell directional buoys
- Moored 6-12 km offshore
- 4 stations > 38 years data
- Sydney > 24 years directional data
- 3 stations > 15 years directional data
- > 230 station years wave data



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## The seiche problem – Coffs Harbour layout



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## Coffs Harbour modes of oscillation (MHL538 1989)

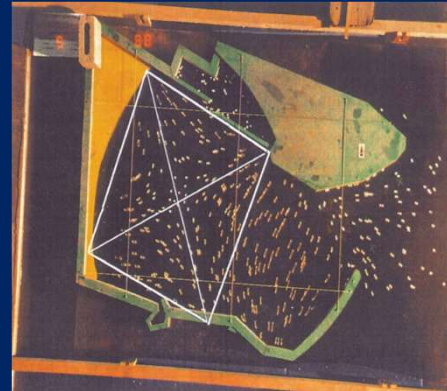
Distorted Scale Model-Erroneous ?-due to error in reflection simulation

136 s seiche

$L_x = 800$



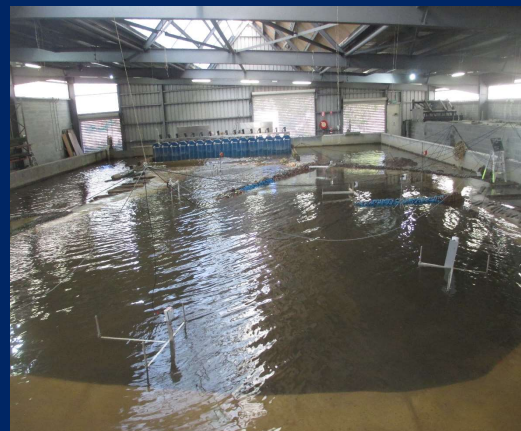
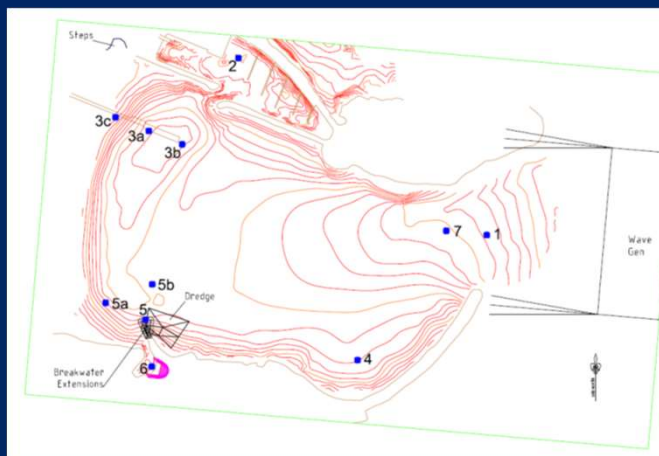
$L_y = 100$



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## Basin layout – scale 1:58 (2014,2020)



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## History of long wave measurement at Coffs Harbour

### Long Wave Measurement History at Coffs Harbour

Source: DWAVE Archive

| Site                | Instrument | Water Depth (m) | First date/<br>Last date | Record Length (years) | Data Capture (%) |
|---------------------|------------|-----------------|--------------------------|-----------------------|------------------|
| Coffs Harbour Jetty | EWS        | 7               | 5/11/86–<br>15/1/96      | 9.2                   | 83.7             |
| Coffs Inner Harbour | EWS        | 4               | 16/1/96–<br>8/10/18      | 22                    | 83.8             |

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## Offshore conditions during extensive seiching at Coffs Harbour

| Date    | Peak Offshore Wave Height (m) | Offshore Wave Period (s) | Comment                                   |
|---------|-------------------------------|--------------------------|---|
| 10/6/12 | 2.06                          | 13.7                     | Seiche indicated on YouTube (section 4.3) |
| 5/9/14  | 4.8                           | 14.85                    | Seiche experienced and reported to CHCC   |

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## Examples of extreme long wave recording in Coffs Harbour

| Date/Time      | Hs   | Hmax | Tp1 | Tp2 |
|----------------|------|------|-----|-----|
| 09/02/88 22:00 | 0.53 | 0.99 | 712 | 109 |
| 15/05/90 08:00 | 0.49 | 0.82 | 712 | 132 |
| 26/04/89 18:00 | 0.40 | 0.62 | 712 | 109 |
| 23/10/92 18:00 | 0.49 | 0.94 | 109 | 66  |
| 09/03/88 22:00 | 0.48 | 0.91 | 109 | 138 |
| 15/05/90 20:00 | 0.46 | 0.84 | 109 | 712 |

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## 128s seiche at Coffs Harbour ramp June 2012

Time 1:27



Time 2:34



<https://www.youtube.com/watch?v=QBqNe36loVw>

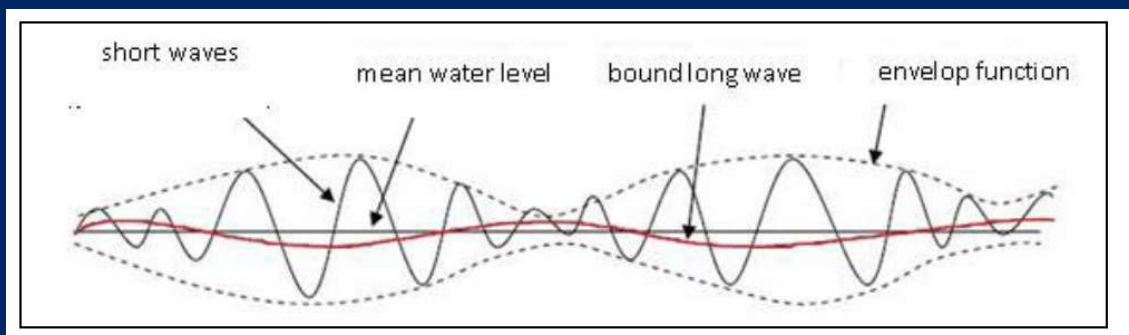
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## Damage due to seiche – NW, NE breakwater crest



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## Forcing function – bounded long wave



Other Forcing functions- (1) Surf beat (2) Bounded long Waves (3) tsunami (4) meteo tsunami-greenspan Proudman forcing (5) Edge waves

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## Periods of oscillation of a closed system – Merian's Formula

The period of oscillation of a seiche in a closed rectangular basin is given by:

$$T = \frac{2/c}{\sqrt{\left(\frac{n}{b}\right)^2 + \left(\frac{m}{l}\right)^2}}$$

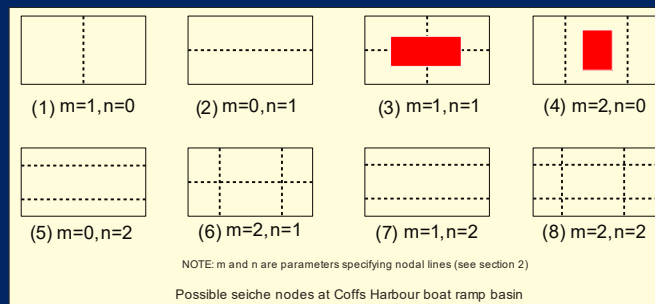
where:

- T = period of oscillation in seconds
- l = length of basin = 1125 m
- b = width of basin = 625 m
- c =  $\sqrt{gd}$  = shallow water celerity
- d = basin depth
- m = number of nodal lines across the basin length
- n = number of nodal lines across the basin width

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## Possible periods of oscillation and modes of oscillation

| Nodal Parameters |   | Oscillation Period (secs) |                 |
|------------------|---|---------------------------|-----------------|
| m                | n | Main Harbour              | Boat Ramp Basin |
| 1                | 0 | 254                       | 36              |
| 0                | 1 | 141                       | 21              |
| 1                | 1 | 123                       | 18              |
| 2                | 0 | 127                       | 18              |
| 0                | 2 | 71                        | 10              |



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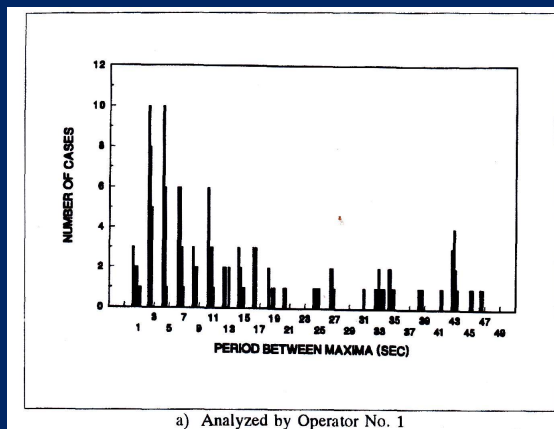


## Testing seiche in boat ramp – original and modified

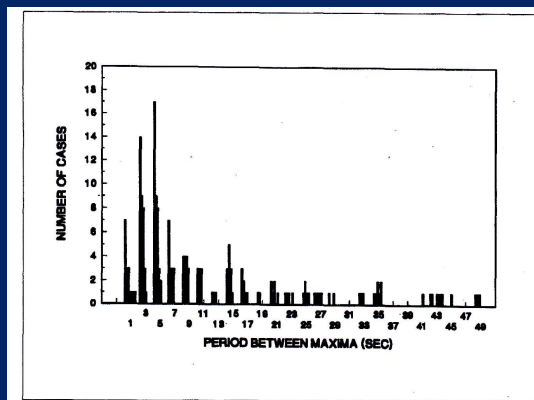


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## Subjective analysis of runup (Briggs, CERC 1991)



a) Analyzed by Operator No. 1

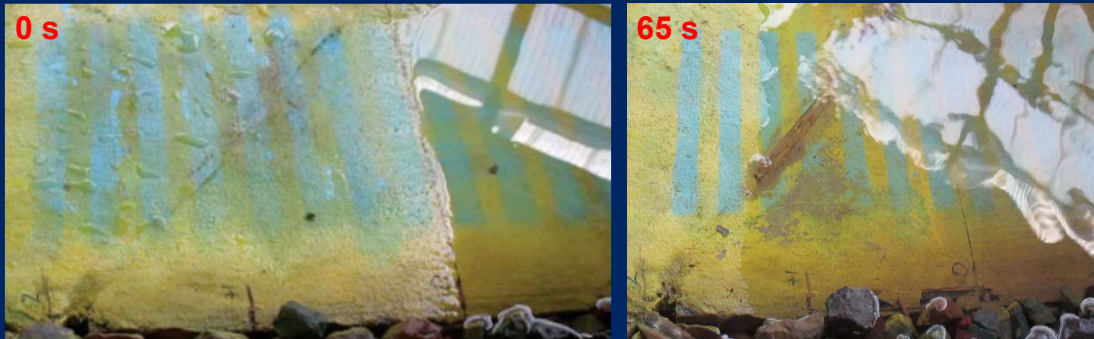


b) Analyzed by Operator No. 2

Figure 5. Distribution of period between successive runup maxima above a threshold value, RUNUP No. 6. Several different thresholds are represented (Continued)

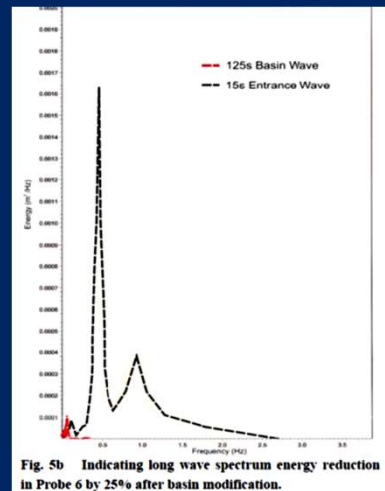
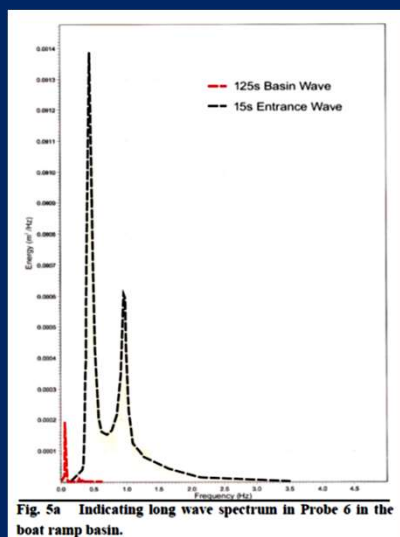
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## Detecting seiche amplitude – runup measurement 130s wave



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## Boat harbour basin wave spectrum vs entrance spectrum – before and after



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## Option 2 Planform change – Raichlan and Poon (MIT 1998, ICCE)



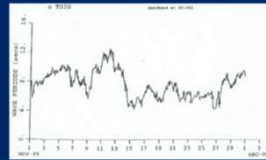
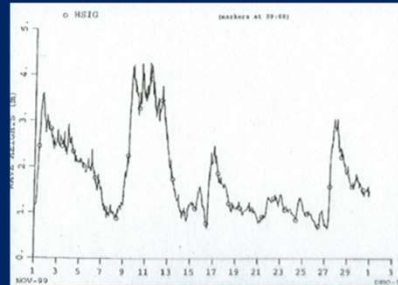
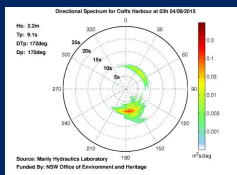
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## Test results – comparison with modified basin

| Water Level (m AHD) | Harbour Entrance |             | Existing Basin |            | Extended Basin |        | Extended Basin (with roughness) |            | Maximum Hsig Reduction (%) |
|---------------------|------------------|-------------|----------------|------------|----------------|--------|---------------------------------|------------|----------------------------|
|                     | Hsig (m)         | Tp (s)      | Hsig (m)       | Tp (s)     | Hsig (m)       | Tp (s) | Hsig (m)                        | Tp (s)     |                            |
| 0.0                 | 4.12             | 17.2        | 0.45           | 125        | 0.39           | 207    | 0.34                            | 623        | 24.5                       |
| 0.8                 | 3.66             | 17.2        | 0.46           | 125        | 0.38           | 104    | 0.35                            | 125        | 23.9                       |
| 0.8                 | 4.40             | 16.4        | 0.56           | 207        | 0.43           | 138    | 0.44                            | 125        | 23.2                       |
| <b>0.8</b>          | <b>4.81</b>      | <b>15.8</b> | <b>0.64</b>    | <b>125</b> |                |        | <b>0.45</b>                     | <b>125</b> | <b>29.7</b>                |
| 0.8                 | 2.78             | 13.2        | 0.44           | 104        |                |        | 0.33                            | 104        | 25.0                       |
| <b>0.8</b>          | <b>2.30</b>      | <b>13.1</b> | <b>0.41</b>    | <b>113</b> |                |        | <b>0.31</b>                     | <b>123</b> | <b>24.4</b>                |
| 0.8                 | 1.38             | 13.3        | 0.25           | 104        |                |        | 0.19                            | 144        | 24.0                       |

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## Forcing by released bound waves ?– Hs=4m-A hand calculation



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## Relevant theory – transfer function of long wave spectra (Sand 1982)

$$\eta_{LB}(t)/h = G_{nm} h \left\{ (a_n a_m + b_n b_m)/h^2 \cos(\Delta\omega_{nm}t - \Delta K_{nm}x_1) + (a_m b_n - a_n b_m)/h^2 \sin(\Delta\omega_{nm}t - \Delta K_{nm}x_1) \right\}$$

$\eta_{LB}(t)$  = time of long wave surface elevations

$h$  = water depth

$G_{nm}$  = non linear transfer function

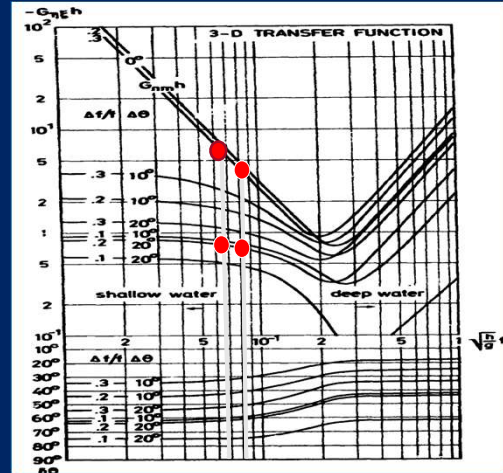
$$\Delta\omega_{nm} = \omega_n - \omega_m$$

$$\Delta K_{nm} = K_n - K_m \text{ for } 10\text{s and } 11\text{s wave long wave of } 110\text{s}$$

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### Directional transfer function for long waves (Sand 1982)

| Date   | Tp | Hs  | $G_{\eta E^h}(20^\circ)$ | $G_{\eta E^h}(0^\circ)$ | $\eta(20^\circ)$ | $\eta(0^\circ)$ |
|--------|----|-----|--------------------------|-------------------------|------------------|-----------------|
| Sep-14 | 15 | 5   | 0.8                      | 7                       | 0.14             | 1.22            |
| Jun-12 | 13 | 2.5 | 0.7                      | 4                       | 0.03             | 0.17            |



### Long Wave Amplitudes (Bowers 1992)

Bound Long Wave- $H_{SI} \sim (H_S T_P)^2$

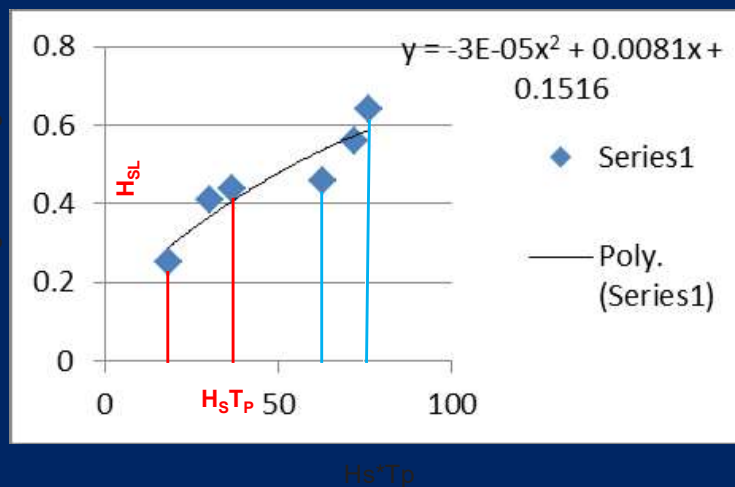
Surf Beat - $H_{SI} \sim H_S T_P$



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### Long wave energy measured at the boat ramp – forcing

- Surf beat
  - Bound long waves
- Bound Long Wave- $H_{SI} \sim (H_S T_P)^2$
- Surf Beat - $H_{SI} \sim H_S T_P$



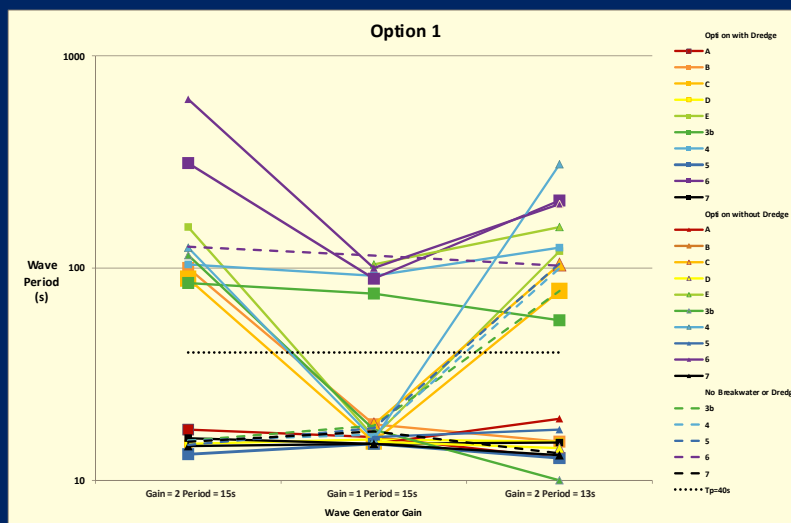
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## Configurations for concept designs – Stage 2



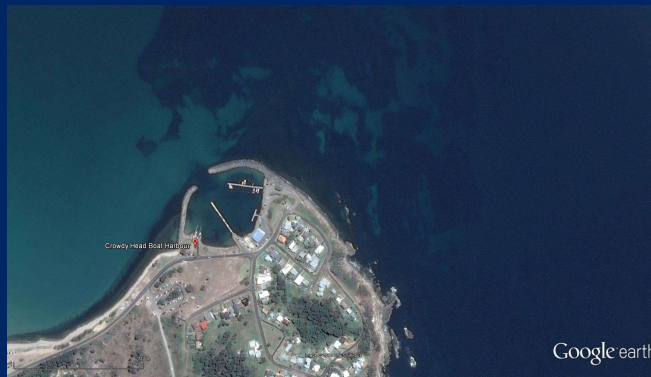
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## Case study for seiche motions for Option 1



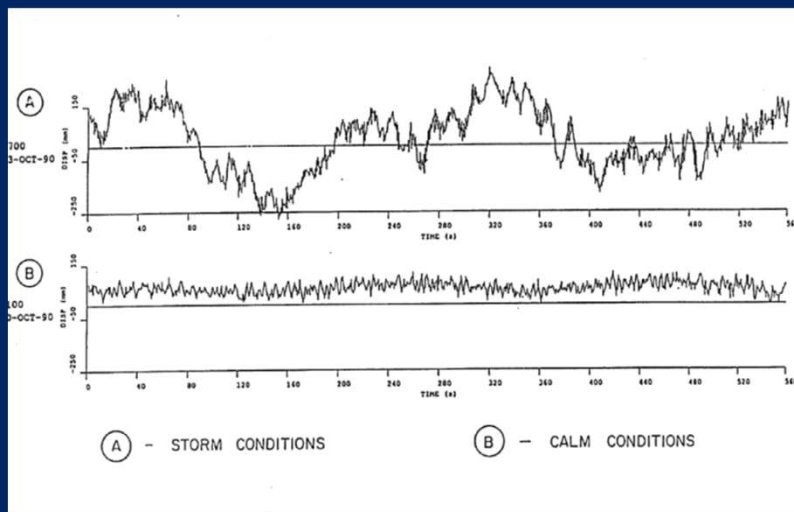
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## Crowdy Head – location and orientation



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## Crowdy Harbour seiche measurement during storm and calm conditions >200s



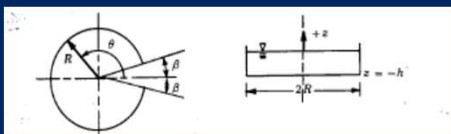
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## Damage due to seiche – Crowdy Harbour – June 2016



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## Oscillations in a circular harbour using cylindrical coordinates – an analytical result



Definition sketch

$$\text{DE: } \nabla^2 \varphi = \nabla^2 \psi = 0 \quad (1)$$

$$\frac{\partial^2 \Phi}{\partial t^2} + g \frac{\partial \Phi}{\partial z} = 0 \quad \text{on } z = 0 \quad (2)$$

BC's

$$\frac{\partial \Phi}{\partial r} = 0 \quad \text{at } r = R \quad 2\pi - \beta > \theta > \beta$$

$$\frac{\partial \Phi}{\partial z} = 0 \quad \text{at } z = -h$$

$$\frac{\partial \Phi}{\partial r} = f(r, \theta, z, t) \quad \text{at } r = R \quad 2\pi - \beta < \theta < \beta$$

Solution

$$\Phi(r, \theta) = \sum_{n=0}^{\infty} A_n J_n(kr) \cos n\theta \quad (3)$$

$$\eta = A_n J_n(kr) \cos n\theta \cos \sigma t$$

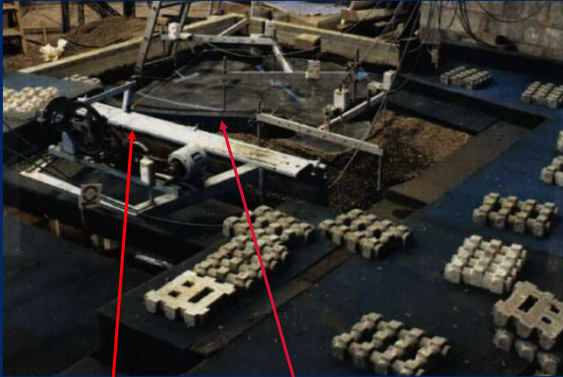
$$kR = 1.841, 5.33, 8.53, \text{ etc.}$$

$$T = 3.41 \frac{R}{\sqrt{gh}}$$

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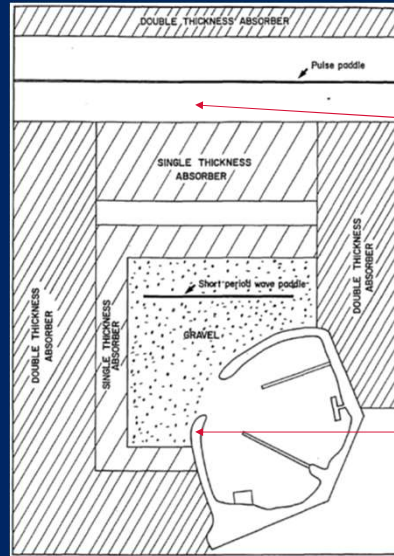


### Distorted scale physical model H 1:100, V 1:50-1994



Short wave paddle

Crowdy Harbour



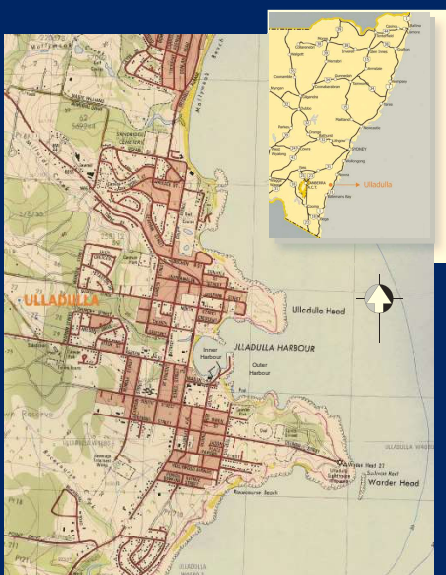
Seiche paddle

Crowdy Harbour



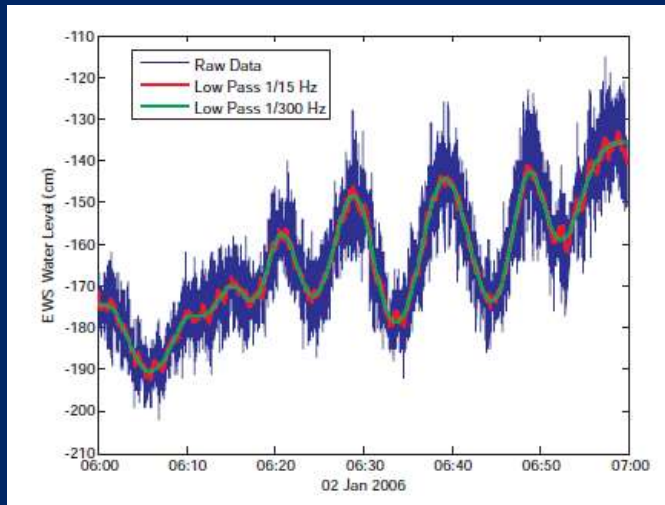
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### Ulladulla Harbour – location and orientation-2006



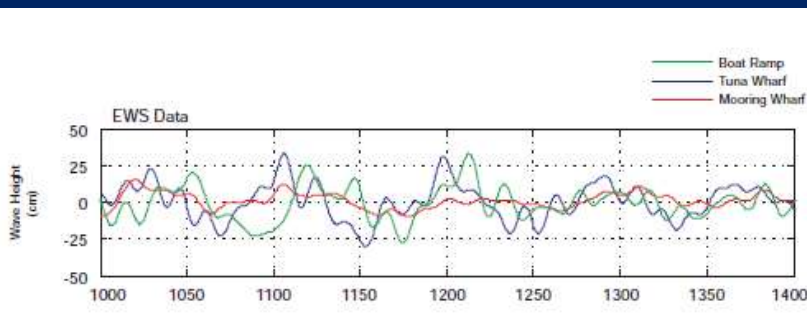
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## Bay oscillations on 2 January 2006 – 600s



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## Measurement of long periods in harbour on 9 April 2006 (83s–91s)

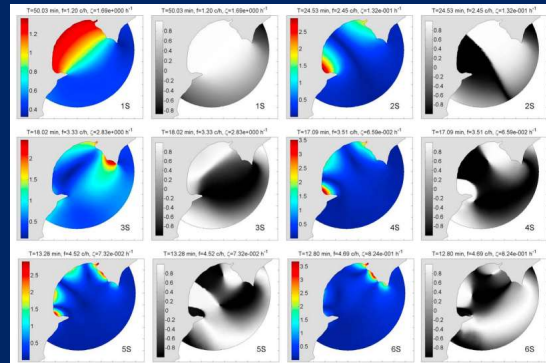


| Site                           | Amplitude   | Phase (secs) | Period (secs) | Correlation Coefficient |
|--------------------------------|-------------|--------------|---------------|-------------------------|
| Boat Ramp EWS                  | 11.1 cm     | 16.8         | 83.9          | 0.792                   |
| Main Wharf EWS                 | 6.9 cm      | - 80.7       | 90.8          | 0.755                   |
| Tuna Wharf EWS                 | 13.3 cm     | 38.6         | 87.6          | 0.874                   |
| Tuna Wharf Cross Shore Current | 3.1 cm/sec  | 39.6         | 87.9          | 0.568                   |
| Tuna Wharf Long Shore Current  | 15.5 cm/sec | - 49.1       | 88.7          | 0.868                   |

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## Empirical Orthogonal Function (EOF) Analysis

- In signal processing, empirical orthogonal function (EOF) analysis finds both time series and spatial patterns.
- A space-time data set (such as numerical model outputs) is decomposed into a set of orthogonal (i.e. statistically independent) space patterns ('EOF') and time-dependent coefficients ('principal components') – e.g. Bellotti et al (2012), Tolkova & Power (2012).
- Decomposition of real-valued EOFs interprets water surface variations within a harbour as a combination of standing waves.
- Fourier analysis of the principal components will all potential resonant frequencies of the harbour basin
- Reconstruction of each EOF mode shows a 'map' of each resonance pattern within the harbour
- Typically, the first resonance pattern is responsible for the largest part of the signal variance, the second for the largest part of the remaining variance, and so on.



Example resonant modes of Poverty Bay, reconstructed from EOF analysis of simulated water level variations during a tsunami. From Bellotti et al., 2012.

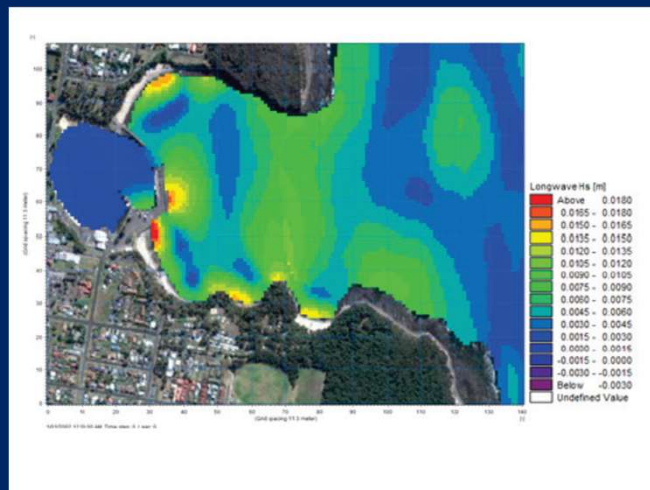
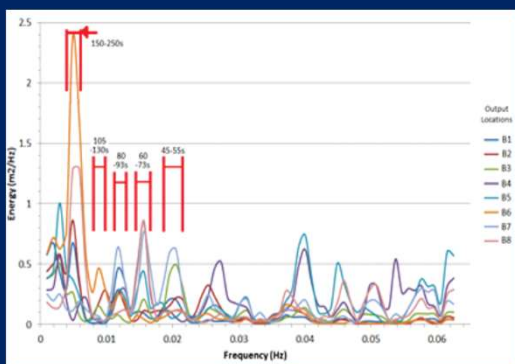
Bellotti, G., Briganti, R. and Beltrami, G.M. (2012). The combined role of bay and shelf modes in tsunami amplification along the coast. *Journal of Geophysical Research* 117, C08027

Tolkova, E. & Power, W. (2011). Obtaining Natural Oscillatory Modes of Bays and Harbours via Empirical Orthogonal Function Analysis of Tsunami Wave Fields. *Ocean Dynamics* 61(6), pp 731 - 751



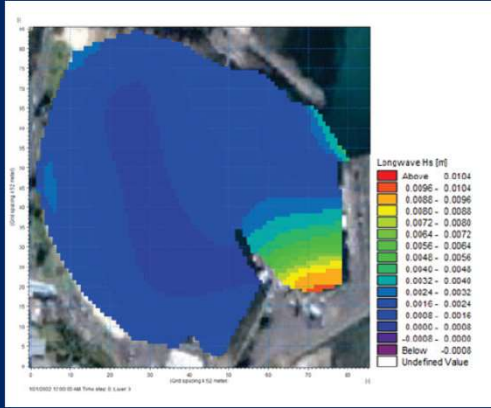
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## White noise forcing of the whole of Ulladulla Bay (80s–93s)

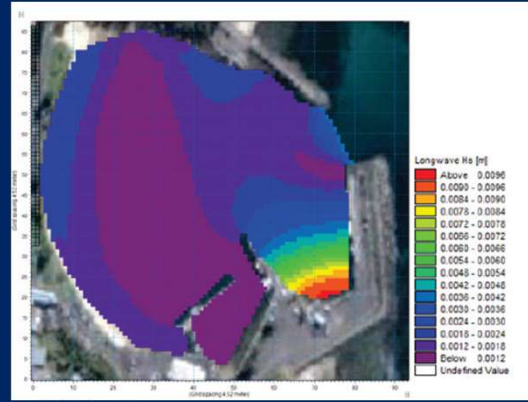


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## White noise forcing (82s–95s) Ulladulla Harbour



Permeable T Jetty



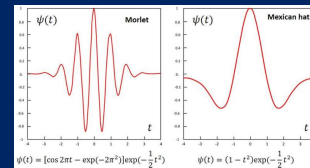
Impermeable T Jetty



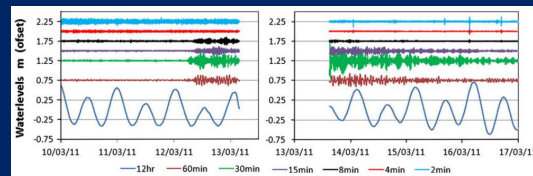
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## Wavelet Analysis

- Fourier analysis: assumes signals are constant with time (“stationary”) - almost never the case within the coastal environment. Infragravity waves are both stochastic and continually evolving with time – “non-stationary”.
- Wavelet analysis: Instead of using sinusoids (as Fourier analysis), a discrete function called the “mother wavelet” is used to decompose (filter) the signal over a wide range of time scales.
- Particularly adept at identifying transient features such as solitary waves or non-stationary processes such as a continually evolving infragravity wave field
- Choice of wavelet shape influences signal reconstruction and statistical estimators (e.g., Bigrelle et al, 2013; Gilles, 2013).
- The closer the wavelet shape is to the underlying signal, the more strongly the wavelet decomposition is able to identify it



Example “Mother Wavelets”



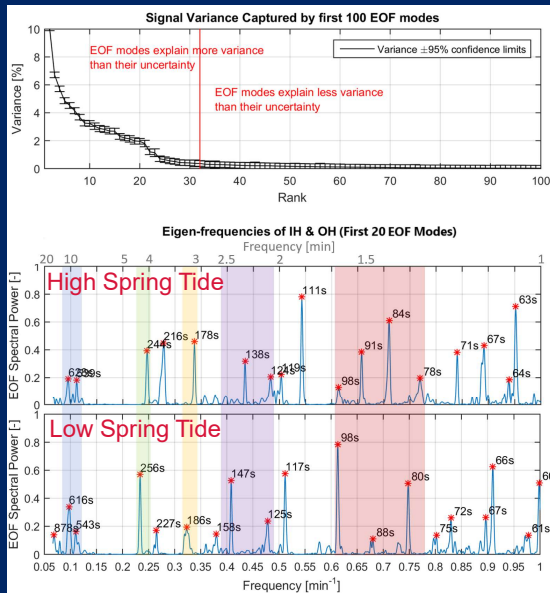
Example wavelet decomposition of water level records within Port Kembla to different frequency bands during the 2011 Japan tsunami. From Hinwood & Luick (2012).

Bigrelle et al (2013). Relevance of Wavelet Shape Selection in a Complex Signal. Mechanical Systems and Signal Processing. 41(2), pp 14 – 33  
 Gilles, J. (2013). Empirical Wavelet Transform. IEEE Transactions on Signal Processing. 61(16), pp 3999 – 4010  
 Hinwood, J. & Luick, J. (2012). Closed Basin Modes of a Dual Basin Harbour. Pure Appl. Geophys., 170(11), 1881 - 1897



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## Port Kembla: EOF Analysis of Resonant Modes from 'White Noise' Simulation

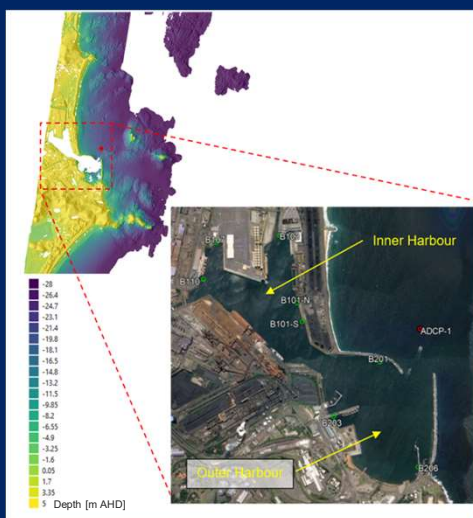


| Observed period (min) | Location and source | Description                    | Predicted period (min) |
|-----------------------|---------------------|--------------------------------|------------------------|
| 1.3                   | IH <sup>a</sup>     | Closed basin mode <sup>b</sup> | 1.33 <sup>a</sup>      |
| 1.2, 1.6              | OH <sup>c</sup>     | —                              | —                      |
| 2.1                   | NTFA <sup>d</sup>   | —                              | —                      |
| 2.4                   | NTFA <sup>d</sup>   | —                              | —                      |
| 2.5                   | OH <sup>e</sup>     | Lenticular mode <sup>f</sup>   | 2.5 <sup>e</sup>       |
| 3                     | OH <sup>a</sup>     | Closed basin mode <sup>g</sup> | 3.15 <sup>a</sup>      |
| 3.1                   | NTFA <sup>d</sup>   | —                              | —                      |
| 4                     | NTFA <sup>d</sup>   | —                              | —                      |
| 8                     | NTFA <sup>d</sup>   | Closed basin mode <sup>h</sup> | 9.0 <sup>i</sup>       |
| 10.5                  | NTFA <sup>d</sup>   | —                              | —                      |



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## Port Kembla: Infragravity Wave Observations & Simulations



Williams, B.G. (2019). Predicting Infragravity Wave Height in Harbours using Artificial Intelligence. Australasian Coasts & Ports 2019 Conference, Hobart

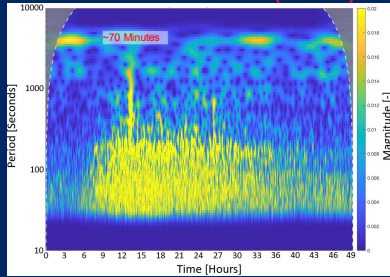
- NSW Ports undertook data collection campaign to measure infragravity wave processes occurring within the Inner and Outer Harbour of Port Kembla, and relate these to meteorology and deep-water swell wave processes (see Williams, 2019)
- Eight RBRsolo<sup>3</sup> pressure transducer data loggers were installed within the Inner and Outer Harbour for a period of approximately one year, sampling continuously at 2Hz.
- Continuous surface elevation data was also collected at the ADCP instrument located approximately 450m north of the Port entrance to determine conditions outside the Port.
- A combination of signal processing and numerical modelling has been undertaken to understand potential resonance patterns within the Inner and Outer Harbour
- A brief analysis of some results is presented in the following slides.



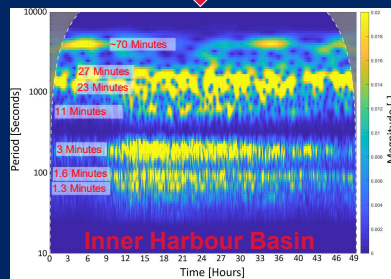
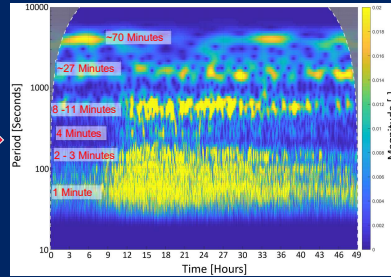
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# Port Kembla: Wavelet Analysis (Magnitude Scalograms)

## Exterior to Harbour (ADCP)



## Outer Harbour Basin



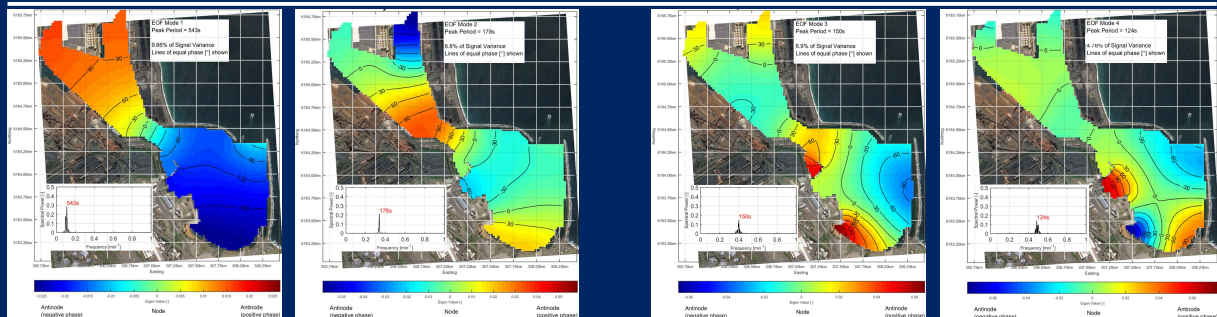
| Observed period (min) | Location and source       | Description                    | Predicted period (min) |
|-----------------------|---------------------------|--------------------------------|------------------------|
| 1.3                   | IH <sup>a</sup>           | Closed basin mode <sup>b</sup> | 1.33 <sup>a</sup>      |
| 1.2, 1.6              | OH <sup>c</sup>           | —                              | —                      |
| 2.1                   | NTFA <sup>d</sup>         | —                              | —                      |
| 2.4                   | NTFA <sup>d</sup>         | —                              | —                      |
| 2.5                   | OH <sup>c</sup>           | Lenticular mode <sup>f</sup>   | 2.5 <sup>e</sup>       |
| 3                     | OH <sup>c</sup>           | Closed basin mode <sup>g</sup> | 3.15 <sup>a</sup>      |
| 3.1                   | NTFA <sup>d</sup>         | —                              | —                      |
| 4                     | NTFA <sup>d</sup>         | —                              | —                      |
| 8                     | NTFA <sup>d</sup>         | Closed basin mode <sup>b</sup> | 9.0 <sup>f</sup>       |
| 10.5                  | NTFA <sup>d</sup>         | —                              | —                      |
| 23.3                  | IH <sup>a</sup>           | Open basin mode <sup>h</sup>   | 22.8 <sup>a</sup>      |
| 23.8                  | NTFA <sup>d</sup>         | —                              | —                      |
| 26.3                  | NTFA <sup>d</sup>         | —                              | —                      |
| 26.6                  | OH <sup>c</sup>           | k                              | —                      |
| 34.5                  | NTFA <sup>d</sup>         | k                              | —                      |
| 60-75                 | Allans Creek <sup>k</sup> | k                              | 55-73 <sup>a</sup>     |
| 67                    | NTFA <sup>d</sup>         | k                              | —                      |

From: Hinwood, J. & Luick, J. (2012). Closed Basin Modes of a Dual Basin Harbour. Pure Appl. Geophys., 170(11), 1881 - 1897



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# Port Kembla: EOF Analysis of Oscillation Modes from White Noise



| Observed period (min) | Location and source | Description                    | Predicted period (min) |
|-----------------------|---------------------|--------------------------------|------------------------|
| 1.3                   | IH <sup>a</sup>     | Closed basin mode <sup>b</sup> | 1.33 <sup>a</sup>      |
| 1.2, 1.6              | OH <sup>c</sup>     | —                              | —                      |
| 2.1                   | NTFA <sup>d</sup>   | —                              | —                      |
| 2.4                   | NTFA <sup>d</sup>   | —                              | —                      |
| 2.5                   | OH <sup>c</sup>     | Lenticular mode <sup>f</sup>   | 2.5 <sup>e</sup>       |
| 3                     | OH <sup>c</sup>     | Closed basin mode <sup>g</sup> | 3.15 <sup>a</sup>      |
| 3.1                   | NTFA <sup>d</sup>   | —                              | —                      |
| 4                     | NTFA <sup>d</sup>   | —                              | —                      |
| 8                     | NTFA <sup>d</sup>   | Closed basin mode <sup>b</sup> | 9.0 <sup>f</sup>       |
| 10.5                  | NTFA <sup>d</sup>   | —                              | —                      |



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## Conclusions

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- Possible modes of oscillation and forcing functions attributable to surf beat from Jetty Beach during mild offshore conditions and bounded long waves during extreme offshore conditions were identified.
- Testing of the above conditions with basin modified resulted in a reduction of less than 30% in long wave energy in the modified boat ramp. This reduction in long wave energy was also measured in the prototype.
- Seiche testing at Crowdy Harbour did not provide a solution to attenuate long waves, however, the short wave model optimised concept designs.
- White noise testing was utilised to indicate the attenuating function of an impermeable jetty in Ulladulla.
- EOF and Wavelet Analysis provided insight into seiche response
- at Port Kembla

